

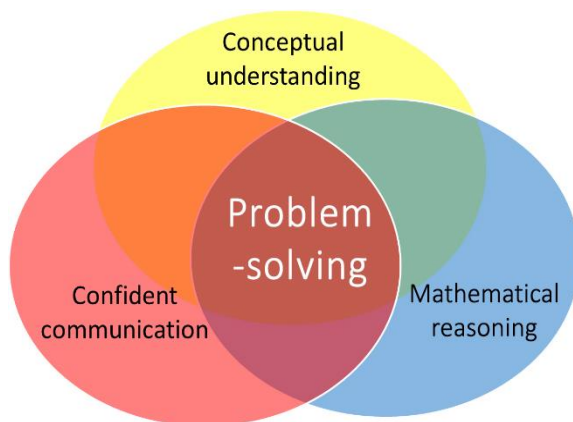
NATURE OF THE ACTIVITIES SUGGESTED HERE

With the surge of interest and sometimes confused interpretations of what is meant by **Mastery** in mathematics, a number of different claims have been made about what it means and what is required. The efficacy of different approaches to implementing a Mastery approach to learning mathematics in the primary school, as demonstrated by higher performing jurisdictions in the Far East, as measured by PISA* and TMSS* have been questioned and challenged.

However, there are some essential points which appear to be in common when examining different approaches.

Research in mathematics education, that curriculum developers and educationalists in the Far East have used, have been known for many years and including Bloom's* theories of *Mastery*, the development of *deeper conceptual understanding* through a progression in *Concrete-Pictorial-Abstract (CPA)* experiences, first discovered by Bruner*, the *realistic mathematics education* of Freudenthal*, and the seminal *Cockcroft Report**, particularly, its emphasis on the importance of *practical experiences* and *problem-solving*. More recently, Lo's* research in the subject of *Variation Theory* has been prominent in exploring how to plan learning for understanding through small steps in conceptual and procedural variation when teaching.

All of these principles have informed the sample of activities presented here. Proponents of Mastery in mathematics (e.g. Drury*) also argue that teaching and learning must focus on enabling children to develop **rich connections** between different facets of their mathematical experience and learning. These aims are also highlighted in the 2014 National Curriculum Aims*. The diagram below shows how these facets are all inter-related, and how teaching to connect these is crucial to **deeper mathematical learning**.



Hence, the activities suggested here are designed to promote the following:

- practical activity manipulating concrete resources where possible;
- working in pairs or groups to encourage the confident use of the language of mathematics through explanation and reasoning with other children;
- ensuring that formal written arithmetic develops from secure experiences with concrete, visual and mental understanding of the manipulation of number and the arithmetic operations;
- solving problems (or by playing games) with the potential for a useful or pleasing result;
- opportunities for finding more than one acceptable result, which children can compare and discuss through collaboration or (guided) peer-assessment.

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There is an expectation that discussion and exploration of misconceptions or errors is a healthy and productive feature of the classroom and that children are encouraged to explain their thinking and listen to others.

In some of the activities, it could be argued that a written sheet of exercises could be given to produce similar results. However, the use of concrete apparatus and visual images provides a medium for discussion and helps to establish a rich conceptual understanding, which is often insufficiently developed through an abstract engagement with written exercises alone. In other cases, children are using equipment to generate the problem to be solved, so can be more engaged in its solution.

Where it is suggested pairs or groups of children work together, the groups may of course be varied to suit the teacher's own judgement. For example, in a game intended for pairs, an odd number of children can be accommodated by a changing combination of 2 vs 1.

To make it more accessible when reading the description of the activities, children's names have been used to identify the sequence of interactions between learners working in pairs or groups.

For every activity, it is paramount that the teacher teaches by modelling the activity with the class, so that children see and imitate what they need to do. Simply providing a written instruction sheet or verbal series of instructions is insufficient for the children to understand and engage with most activities.

Each activity has suggestions for extending or simplification. The expectation is that each can be explored comprehensively within one classroom lesson of 45 minutes or more.

For more information about improving the capacity for teaching and learning mathematics in the primary school, visit www.MathematicsMastered.org

*References

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Lo, M. L. (2012) *Variation Theory and the Improvement of Teaching and Learning*, Gothenburg studies in educational sciences 323, Gothenburg University.

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19. Algebraic Reasoning

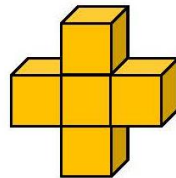
To develop a simple formula to generalise a linear number sequence.

This is a practical exercise for exploring number patterns to find a simple formula for generalising a linear number sequence.

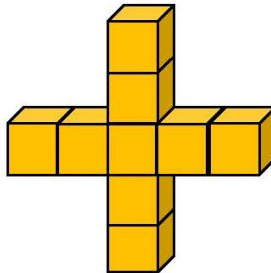
Generalising sequences Work in groups of 3 or 4, to discuss and share ideas. They will need access to:

- A class set of *multilink* cubes, or some counters.

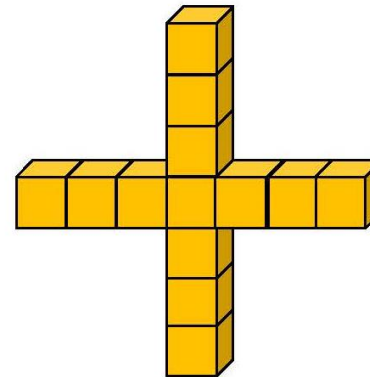
Start by asking Charlie, Meena, Alexi and Woljca to make the following sequence of shapes:



1st



2nd



3rd

What do they think the 4th and 5th shapes would look like? Ask them to make them?

How many cubes are there in each shape? (5, 9, 13, 17, 21)

Could they work out how many cubes they would need to make the 6th shape, without making it? (add 4 to the 5th shape)

How many would they need to make 10th shape? (add another 4×4)

Do children see that each shape is established by adding 4 to the previous shape?

Can they write a similar calculation for each shape in terms of the number of times they need to add 4?

If they cannot derive the formula, can they describe verbally the increment to make each successive shape, and work out the number of cubes needed for a specific shape, e.g. the 10th?

Suppose we wanted to make the n^{th} shape? If n could be any whole number, could they describe a *formula*: a rule to work out how many cubes they would need?

1st shape needs 5 cubes = $1 + (4 \times \underline{1})$

2nd “ “ 9 cubes = $1 + (4 \times \underline{2})$

3rd “ “ 13 cubes = $1 + (4 \times \underline{3})$

4th “ “ 17 cubes = $1 + (4 \times \underline{4})$

Highlight the part of the calculation which changes with each shape and ask if they can see any connection with the changing part and the number of the shape (called the *term* of the sequence). Suppose this was any number in the sequence, n ?

n^{th} shape needs $1 + (4 \times n)$ or $1 + 4n$ cubes

(Explain that we can write the multiplication $4 \times n$ simply as $4n$.)

To extend the challenge, can they create their own simple sequence of a pattern of shapes that increases by the same number each time, and challenge others in their group to work out their formula?